MPRI

Abstract interpretation of protein-protein interactions networks

Jérôme Feret

DI - ÉNS

`kappalanguage.org`

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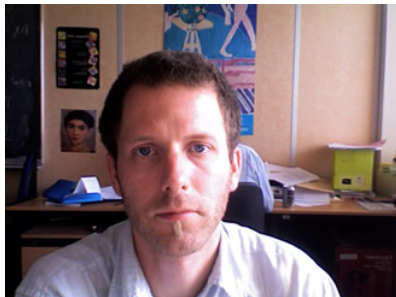
Joint-work with...

Walter Fontana
Harvard Medical School

Vincent Danos
ÉNS
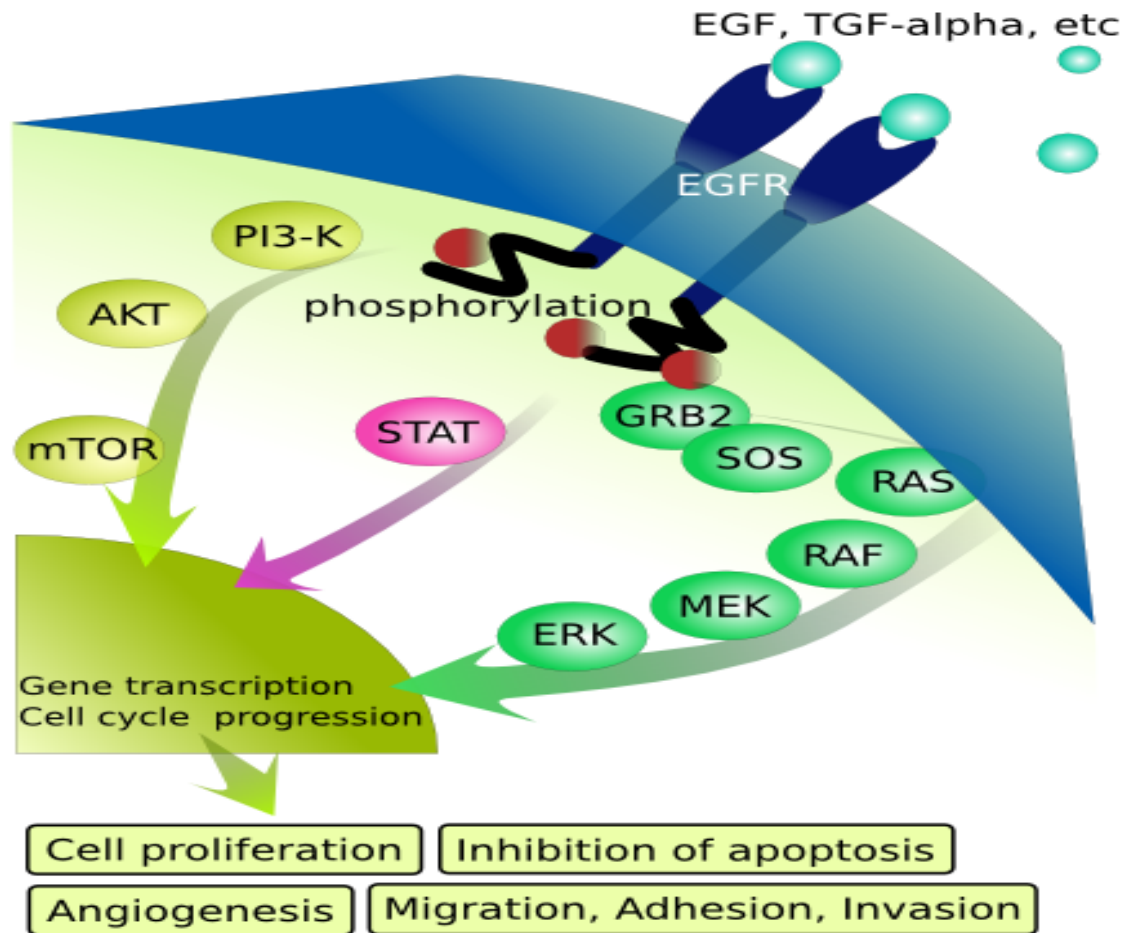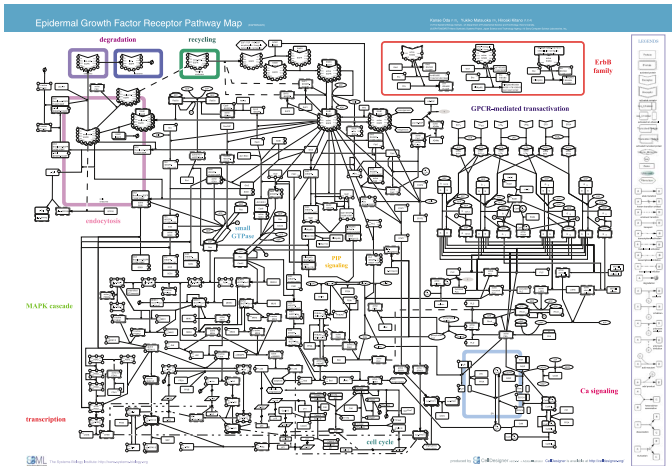
Ferdinanda Camporesi
Bologna / ÉNS

Russ Harmer
ÉNS Lyon

Jean Krivine
Paris VII

Signalling Pathways

Eikuch, 2007
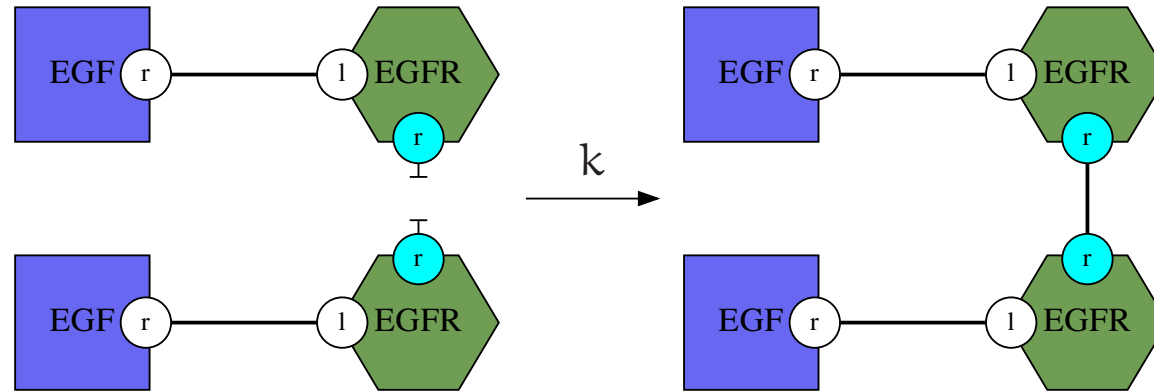
Bridging the gap between...

$$\begin{cases}
\frac{dx_1}{dt} = -k_1 \cdot x_1 \cdot x_2 + k_{-1} \cdot x_3 \\
\frac{dx_2}{dt} = -k_1 \cdot x_1 \cdot x_2 + k_{-1} \cdot x_3 \\
\frac{dx_3}{dt} = k_1 \cdot x_1 \cdot x_2 - k_{-1} \cdot x_3 + 2 \cdot k_2 \cdot x_3 \cdot x_3 - k_{-2} \cdot x_4 \\
\frac{dx_4}{dt} = k_2 \cdot x_3^2 - k_2 \cdot x_4 + \frac{v_4 \cdot x_5}{p_4 + x_5} - k_3 \cdot x_4 - k_{-3} \cdot x_5 \\
\frac{dx_5}{dt} = \cdots \\
\quad \vdots \\
\frac{dx_n}{dt} = -k_1 \cdot x_1 \cdot c_2 + k_{-1} \cdot x_3
\end{cases}$$
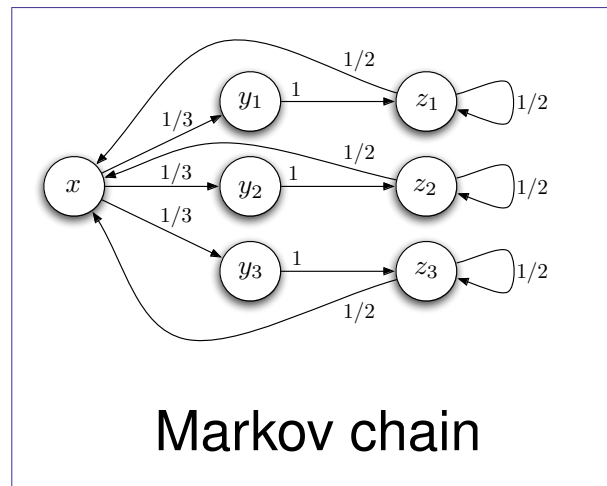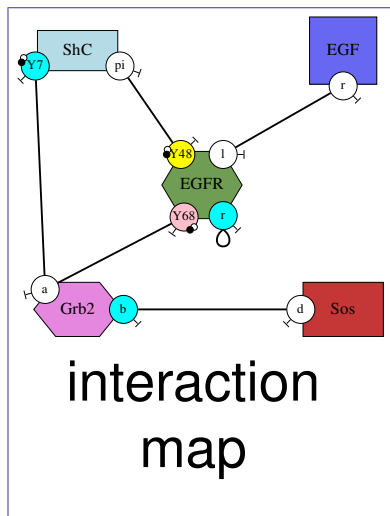
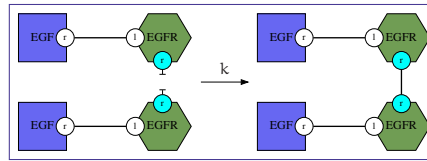**knowledge representation** **and** **models of the behaviour of systems**

Site-graphs rewriting

- a language close to knowledge representation;
- rules are easy to update;
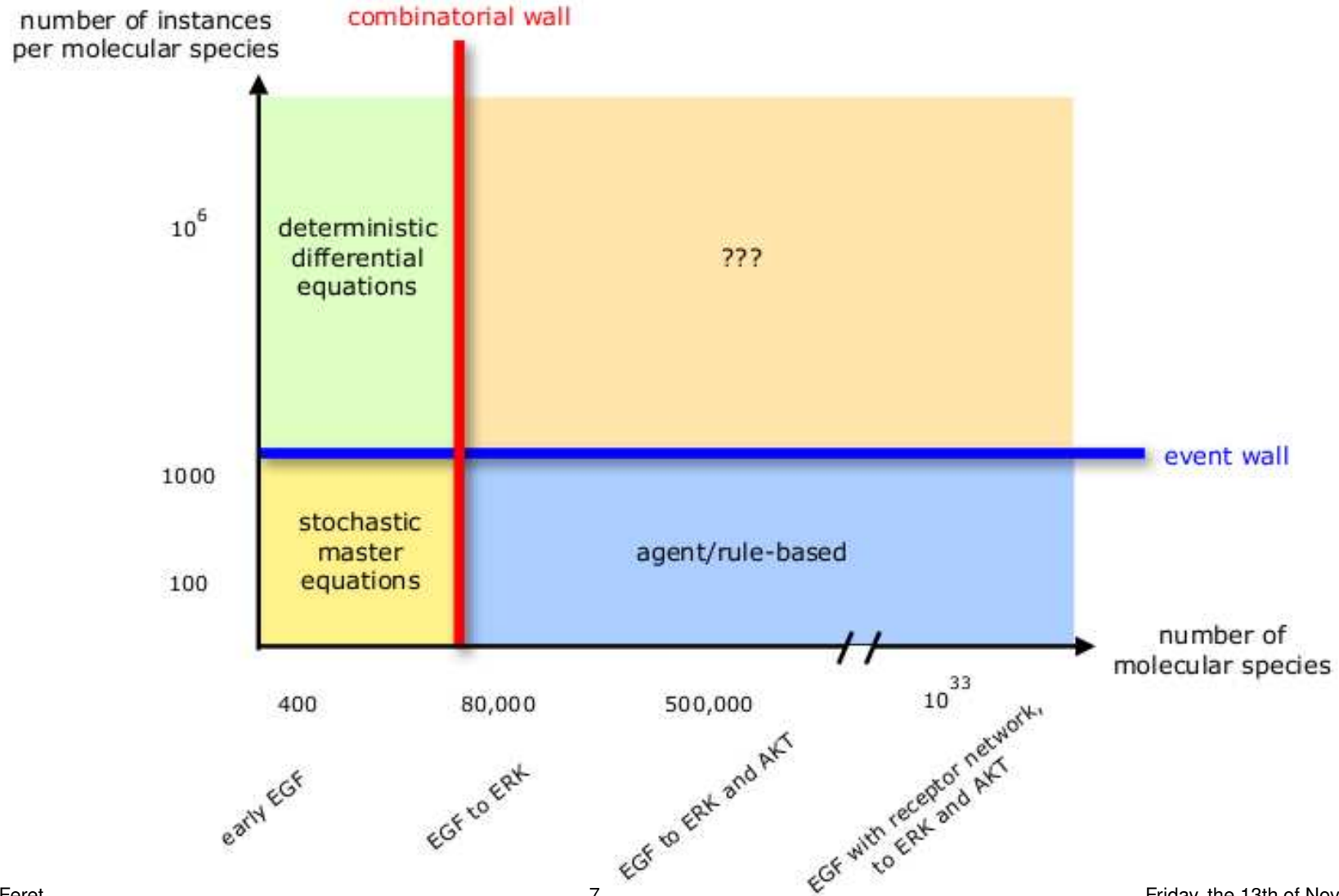- a compact description of models.

Choices of semantics
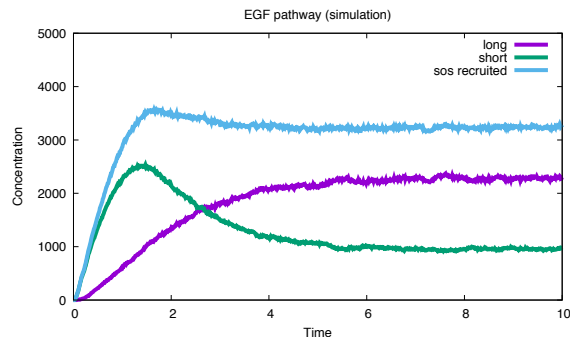

interaction map

Markov chain

$$\begin{cases} \frac{dx_1}{dt} = -k_1 \cdot x_1 \cdot x_2 + k_{-1} \cdot x_3 \\ \frac{dx_2}{dt} = -k_1 \cdot x_1 \cdot x_2 + k_{-1} \cdot x_3 \\ \frac{dx_3}{dt} = k_1 \cdot x_1 \cdot x_2 - k_{-1} \cdot x_3 + 2 \cdot k_2 \cdot x_3 \cdot x_3 - k_{-2} \cdot x_4 \\ \frac{dx_4}{dt} = k_2 \cdot x_3^2 - k_2 \cdot x_4 + \frac{v_4 \cdot x_5}{p_4 + x_5} - k_3 \cdot x_4 - k_{-3} \cdot x_5 \\ \frac{dx_5}{dt} = \cdots \\ \qquad \vdots \\ \frac{dx_n}{dt} = -k_1 \cdot x_1 \cdot c_2 + k_{-1} \cdot x_3 \end{cases}$$
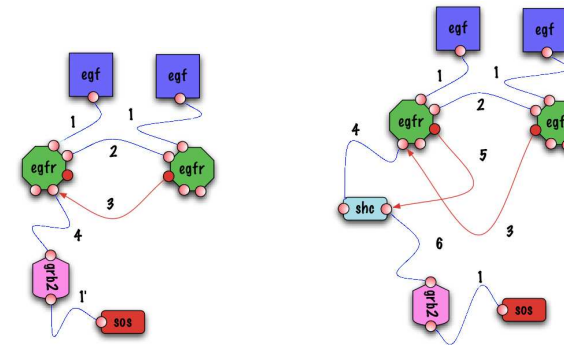
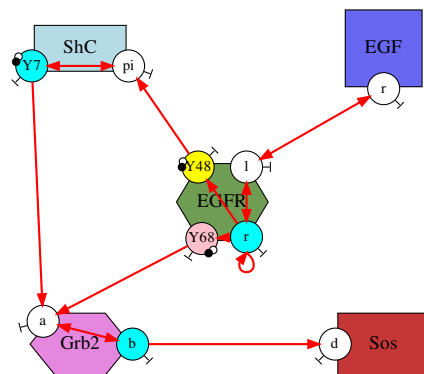ordinary differential equations

Complexity walls

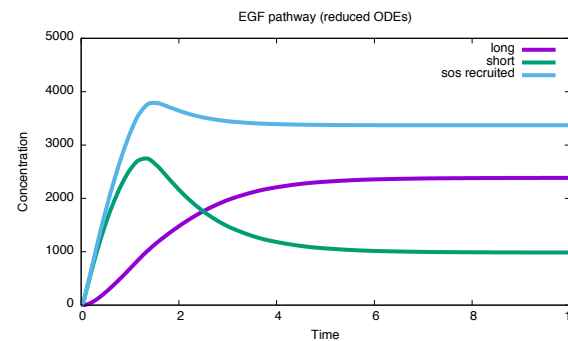# Abstractions offer different perspectives on models

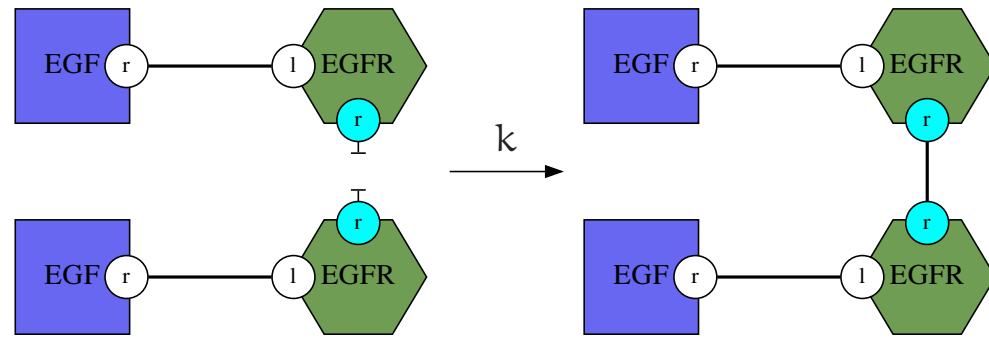concrete semantics

causal traces

information flow

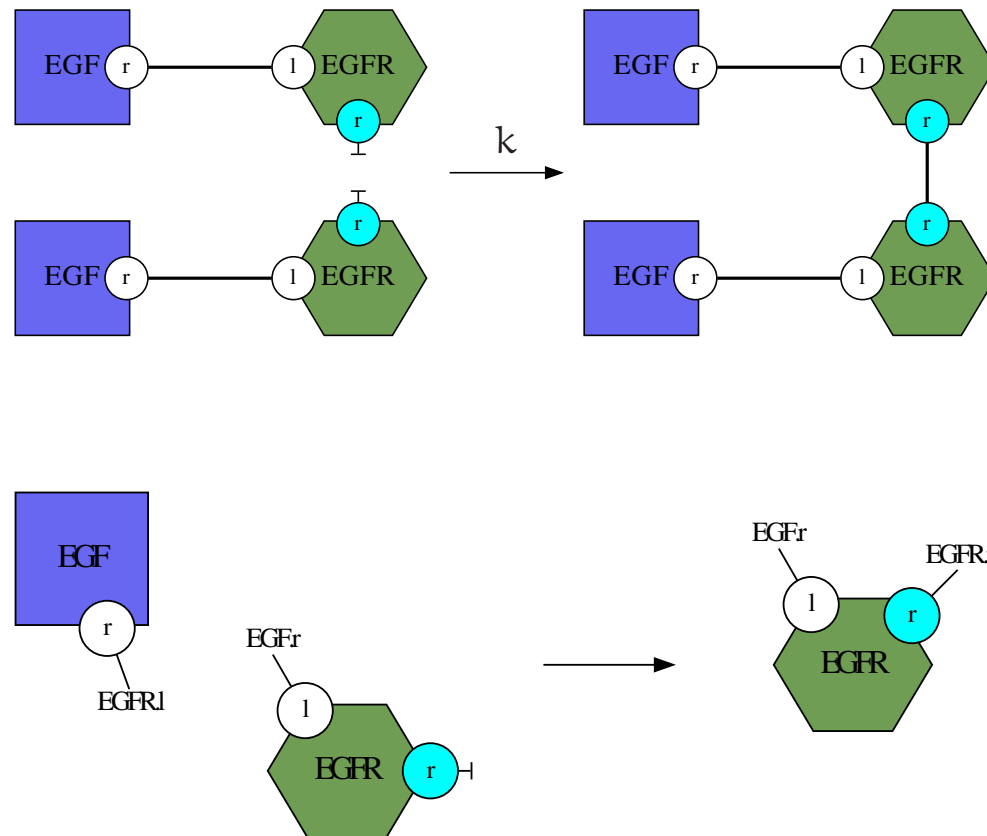exact projection
of the ODE semantics

Static analysis of reachable species (I/II)

We capture the relationships between the states of the sites of each agent.

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# Static analysis of reachable species (II/II)

Applications:

1. check the consistency of a model [ICCMSE'07]

2. compute the properties to allow fast simulation [APLAS'07]

3. simplify models,

4. compute independent fragments of chemical species [PNAS'09, LICS'10,Chaos'10]

The analysis is complete (no false positif) for a significatif kernel of Kappa [VMCAI'08].

Model reduction

The ground differential system uses one variable per chemical species;
We directly compute its exact projection over independent fragments of chemical species.
With a small model, 356 chemical species are reduced into 38 fragments:
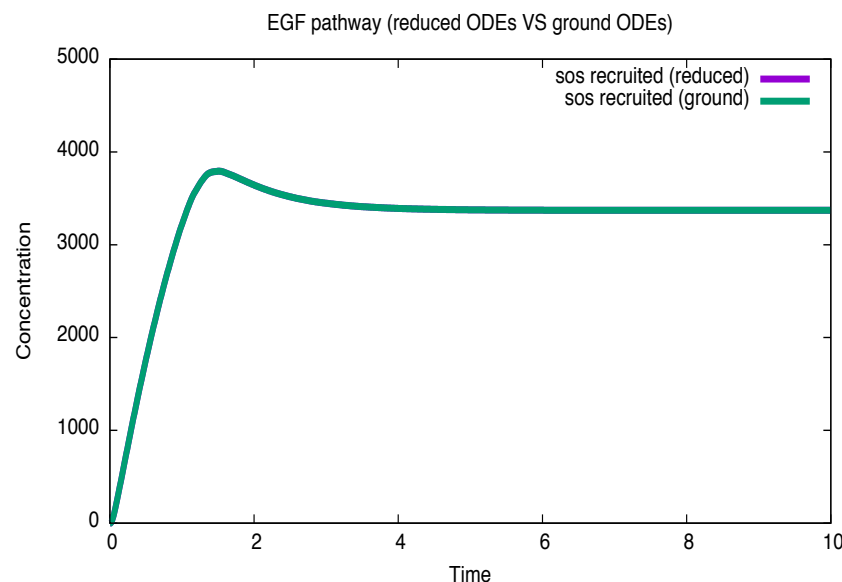
On a bigger model, 10^{19} chemical species are reduced into 180 000 fragments. [PNAS'09,LICS'10,Chaos'10]