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Guaranteeing Timed Opacity using Parametric Timed Model Checking

Étienne André¹, Didier Lime², Dylan Marinho¹ and Sun Jun³

 1 Université de Lorraine, CNRS, Inria, LORIA, Nancy, France 2 École Centrale de Nantes, LS2N, UMR CNRS 6004, Nantes, France

³ School of Information Systems, Singapore Management University, Singapore

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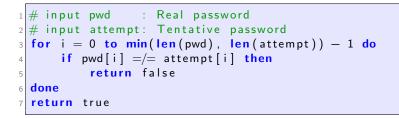
Context: timing attacks

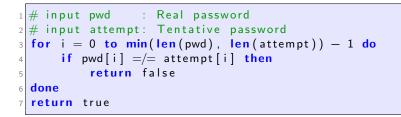
 Principle: deduce private information from timing data (execution time)

Issues:

- May depend on the implementation (or, even worse, be introduced by the compiler)
- A relatively trivial solution: make the program last always its maximum execution time Drawback: loss of efficiency

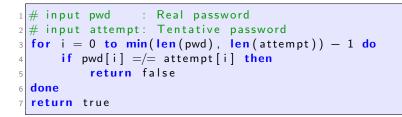
 \rightsquigarrow Non-trivial problem

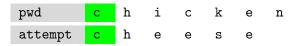




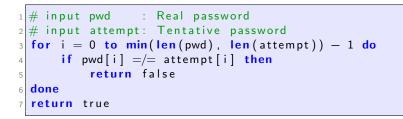
pwd	с	h	i	с	k	е	n
attempt	с	h	е	е	s	е	

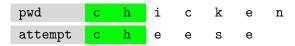
Execution time:



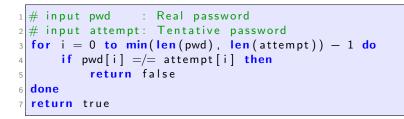


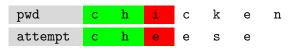
Execution time: ϵ



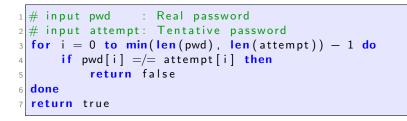


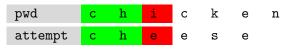
Execution time: $\epsilon + \epsilon$





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Problem: The execution time is proportional to the number of consecutive correct characters from the beginning of attempt

Informal problems

Question: can we exhibit secure execution times?

Time-opacity computation

Exhibit execution times for which it is not possible to infer information on the internal behavior

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Time-opacity computation

Exhibit execution times for which it is not possible to infer information on the internal behavior

Further question: can we also tune internal timing constants to make the system resisting to timing attacks?

Time-opacity synthesis

Exhibit execution times and internal timing constants for which it is not possible to infer information on the internal behavior

Outline

Formalism and Computation results

Toward parameter synthesis

Experiments

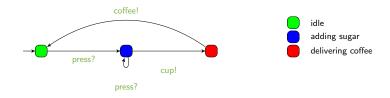
Perspectives

Finite state automaton (sets of locations)



[[]AD94] Rajeev Alur and David L. Dill. "A theory of timed automata". In: Theoretical Computer Science 126.2 (Apr. 1994), pp. 183–235. ISSN: 0304-3975. DOI: 10.1016/0304-3975(94)90010-8

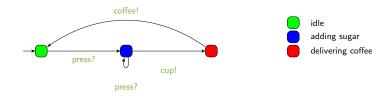
Finite state automaton (sets of locations and actions)



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Finite state automaton (sets of locations and actions) augmented with a set X of clocks [AD94]

Real-valued variables evolving linearly at the same rate



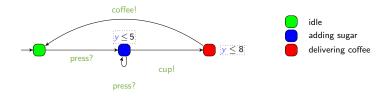
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 Finite state automaton (sets of locations and actions) augmented with a set X of clocks
[AD94]

- Real-valued variables evolving linearly at the same rate
- Can be compared to integer constants in invariants

Features

Location invariant: property to be verified to stay at a location



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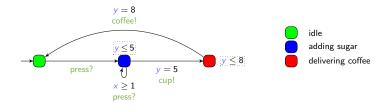
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Transition guard: property to be verified to enable a transition



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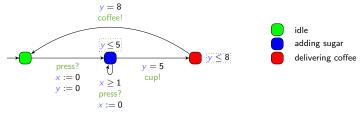
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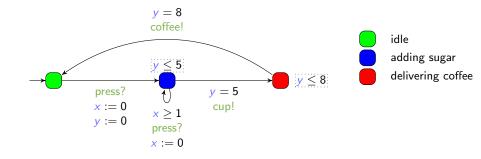
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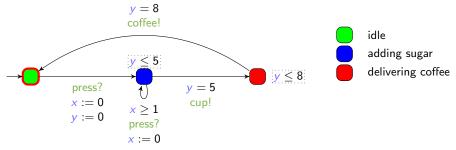
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Clock reset: some of the clocks can be set to 0 along transitions



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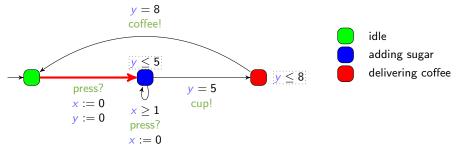




Example of concrete run for the coffee machine

Coffee with 2 doses of sugar

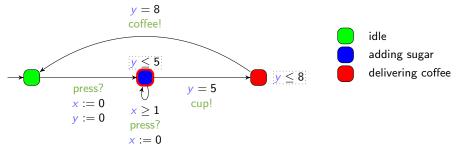
 $\begin{array}{c} x = & 0 \\ y = & 0 \end{array}$



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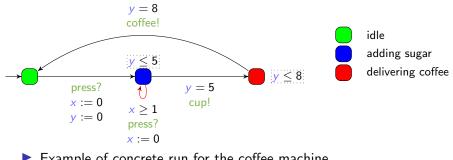




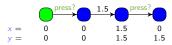
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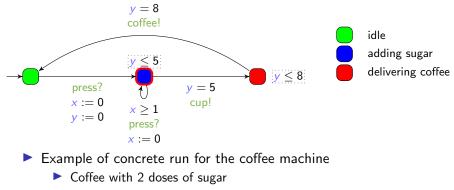
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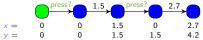


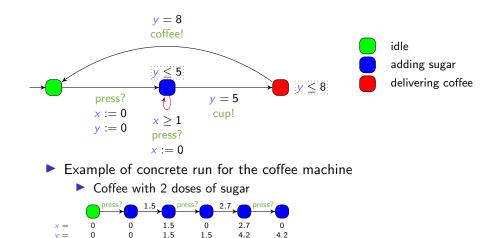


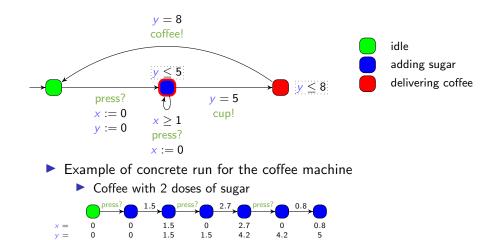
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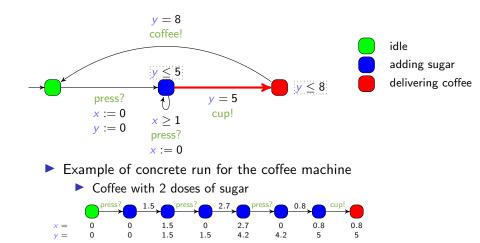


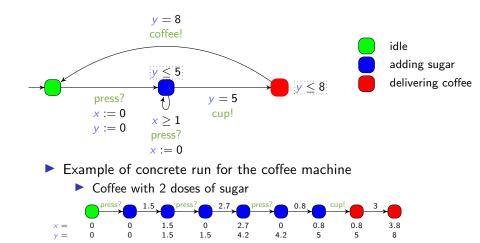


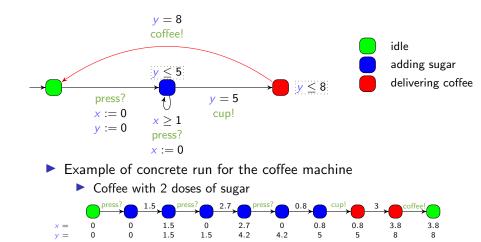








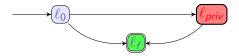




Formalization

Hypotheses:

- A start location ℓ_0 and an end location ℓ_f
- ► A special private location ℓ_{priv}

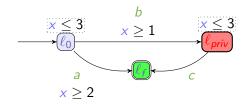


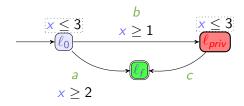
Definition (timed opacity)

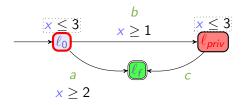
The system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f for a duration d if there exist two runs to ℓ_f of duration d

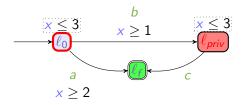
- 1. one passing by $\ell_{\textit{priv}}$
- 2. one *not* passing by ℓ_{priv}

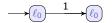
[[]AS19] Étienne André and Jun Sun, "Parametric Timed Model Checking for Guaranteeing Timed Opacity". In: ATVA (Oct. 28–31, 2019). Ed. by Yu-Fang Chen, Chih-Hong Cheng, and Javier Esparza. Vol. 11781. Lecture Notes in Computer Science. Taipei, Taiwan: Springer, 2019, pp. 115–130. DOI: 10.1007/978-3-030-31784-3_7

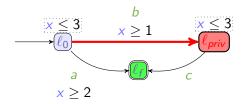


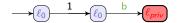


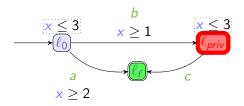




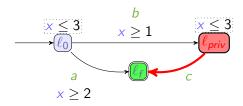


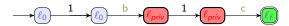


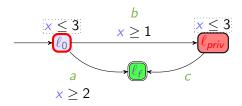




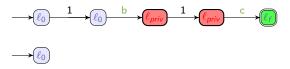


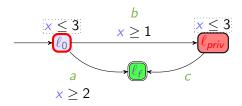




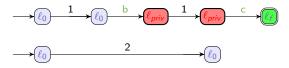


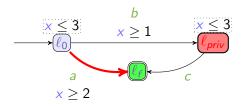
• There exist two runs of duration d = 2:



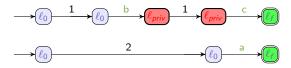


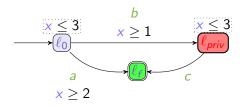
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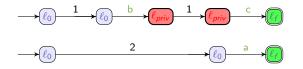


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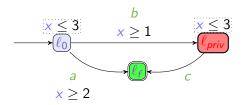




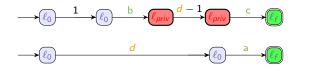
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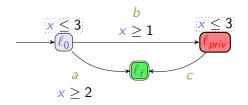
We say that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f for a duration d = 2



There exist two runs of duration d for all durations $d \in [2,3]$:

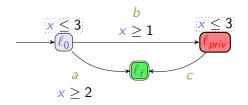


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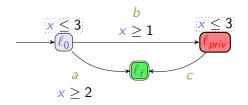
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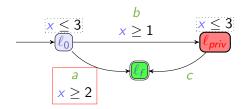




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► But There exists a run of duration 1.5 passing by ℓ_{priv} $\rightarrow \ell_0$ $\stackrel{1}{\longrightarrow} \ell_0$ $\stackrel{b}{\longrightarrow} \ell_{priv}$ $\stackrel{0.5}{\longrightarrow} \ell_{priv}$ $\stackrel{c}{\longrightarrow} \ell_{priv}$

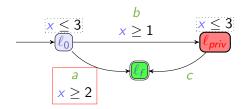


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We say that the system is *not* fully opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Problem 1: timed-opacity computation

Timed-opacity computation problem

Find durations *d* ("execution times") of runs from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

Theorem The durations *d* such that the system is opaque can be effectively computed and defined

[[]TOSEM22] Étienne André, Didier Lime, Dylan Marinho, and Jun Sun. "Guaranteeing Timed Opacity using Parametric Timed Model Checking". In: TOSEM (2022). To appear

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Corollary Asking if a TA is opaque for all its execution times is decidable

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Proof: based on the region graph and RA-arithmetic (see [TOSEM22])

Exact complexity: unproved (EXPSPACE upper bound proved, but exponential hardness seems likely)

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Outline

Formalism and Computation results

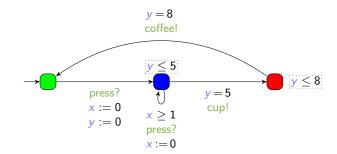
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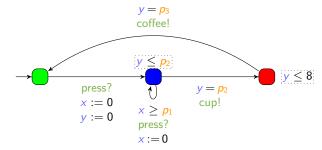
Timed automaton (sets of locations, actions and clocks)



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Parametric Timed Automaton (PTA)

- Timed automaton (sets of locations, actions and clocks) augmented with a set P of parameters [AHV93]
 - Unknown constants compared to a clock in guards and invariants



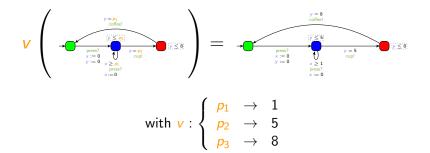
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Valuation of a PTA = TA

Given a PTA A and a parameter valuation v,
v(A) is the TA where each parameter p is valuated by v(p)

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Timed-opacity synthesis problem

Find durations *d* ("execution times") of runs of \mathcal{A} from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

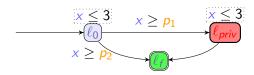
Timed-opacity synthesis problem

Find parameter valuations v and durations d ("execution times") of runs of v(A) from ℓ_0 to ℓ_f such that the system is opaque w.r.t. ℓ_{priv} on the way to ℓ_f

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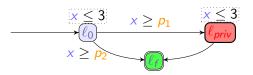
Example:



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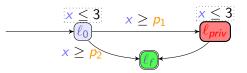
Expected result:

 $p_1 \leq 3 \land p_2 \leq 3 \land d \in [p_2, 3]$

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Example:



Expected result: $p_1 \leq 3 \land p_2 \leq 3 \land d \in [p_2, 3]$ If $v(p_1) = 1$ and $v(p_2) = 2$: $\top \land \top \land d \in [2, 3]$

Overview of our theoretical results

 General case: The mere existence of a parameter valuation for which there exists a duration for which timed-opacity is achieved is undecidable

[TOSEM22]

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- Study of a subclass known for being "at the frontier" of decidability (L/U-PTA)
 - The existence of valuations for timed opacity w.r.t. some execution times is decidable
 - The existence of valuations for full timed opacity is undecidable
 - The synthesis is uncomptable in pratice

[TOSEM22]

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[TOSEM22]

We adopt a "best-effort" approach for the general case of PTAsApproach not guaranteed to terminate in theory

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Outline

Formalism and Computation results

Toward parameter synthesis

Experiments

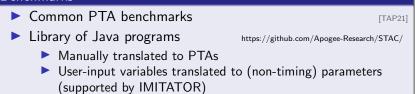
Perspectives

Experimental environment

Algorithms

- 1. Timed-opacity: "for a non-parametric TA, is the TA opaque for all execution times?"
- 2. Timed-opacity synthesis: "for a PTA, synthesize parameter valuations and execution times ensuring timed opacity"

Benchmarks



See experiments at doi.org/10.5281/zenodo.3251141

and imitator.fr/static/ATVA19/

Experiments:	(non-parametric)	timed o	pacity

Model	,		Transf. PTA		PTA	Result	
Name	$ \mathcal{A} $	X	$ \mathcal{A} $	X	P	Time (s)	Opaque?
Fig. 5, [VNN18]	1	1	2	3	3	0.02	(×)
Fig. 1b, [GMR07]	1	1	2	3	1	0.04	(×)
Fig. 2a, [GMR07]	1	1	2	3	1	0.05	(×)
Fig. 2b, [GMR07]	1	1	2	3	1	0.02	(\times)
Web privacy problem [Ben+15]	1	2	2	4	1	0.07	(×)
Coffee	1	2	2	5	1	0.05	\checkmark
Fischer-HSRV02	3	2	6	5	1	5.83	(×)
STAC:1:n			2	3	6	0.12	(×)
STAC:1:v			2	3	6	0.11	×
STAC:3:n			2	3	8	0.72	\checkmark
STAC:3:v			2	3	8	0.74	(×)
STAC:4:n			2	3	8	6.40	×
STAC:4:v			2	3	8	265.52	×
STAC:5:n			2	3	6	0.24	
STAC:11A:v			2	3	8	47.77	(×)
STAC:11B:v			2	3	8	59.35	(×)
STAC:12c:v			2	3	8	18.44	×
STAC:12e:n			2	3	8	0.58	×
STAC:12e:v			2	3	8	1.10	(×)
STAC:14:n			2	3	8	22.34	(×)

 $\surd =$ not vulnerable; (\times) = vulnerable, can be repaired; $\times =$ vulnerable, cannot be repaired

Experiments: (parametric) timed-opacity synthesis

Model			Transf. PTA		Result			
Name	$ \mathcal{A} $	X	P	$ \mathcal{A} $	X	P	Time (s)	Constraint
Fig. 5, [VNN18]	1	1	0	2	3	4	0.02	K
Fig. 1b, [GMR07]	1	1	0	2	3	3	0.03	K
Fig. 2, [GMR07]	1	1	0	2	3	3	0.05	K
Web privacy problem [Ben+15]	1	2	2	2	4	3	0.07	K
Coffee	1	2	3	2	5	4	0.10	Т
Fischer-HSRV02	3	2	2	6	5	3	7.53	K
STAC:3:v			2	2	3	9	0.93	K

- K = some valuations make the system non-vulnerable;
- $\mathsf{T} = \mathsf{all}$ valuations make the system non-vulnerable

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Perspectives

On the theoretical side

- Some restricted problems remain open e.g., PTA with one clock
- Study more restrictive sub-classes, with the hope to exhibit a decidable one

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- Study more restrictive sub-classes, with the hope to exhibit a decidable one

On the pratical side

Have an automatic translation of programs to PTAs

 \rightarrow Some experiments were done, but on Java programs manually translated to PTAs

Repairing a non-opaque system

 \rightarrow Preliminary ideas in ${\rm [TOSEM22]}^a,$ but not fixed

^a[TOSEM22] Étienne André, Didier Lime, Dylan Marinho, and Jun Sun. "Guaranteeing Timed Opacity using Parametric Timed Model Checking". In: *TOSEM* (2022). To appear

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